









 $= b_1$

 $= b_{\gamma}$

 $= b_{n}$













| | Finding Dual of a L | P problemcontd. | | | | | |
|----|---|---|--|--|--|--|--|
| | Primal | Dual | | | | | |
| | ith variable unrestricted | ith constraint with = sign | | | | | |
| | jth constraint with = sign | jth variable unrestricted | | | | | |
| | RHS of jth constraint | Cost coefficient associated with j th variable in the objective function | | | | | |
| | Cost coefficient associated with i th variable in the objective function | RHS of i th constraint | | | | | |
| | | | | | | | |
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| | Di st | ual Simplex Method: Iterative epscontd. | | | | | | |
|----|--|--|--|--|--|--|--|--|
| 1 | 5. Pivotal operation: Pivotal operation is exactly same as in the case of simplex method, considering the pivotal element as the element at the intersection of pivotal row and pivotal column. | | | | | | | |
| | 6. | Check for optimality: If all the basic variables have nonnegative values then the optimum solution is reached. Otherwise, Steps 3 to 5 are repeated until the optimum is reached. | | | | | | |
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| | Dual Simplex Method: An Example |
|----|---|
| C | Consider the following problem: |
| | Minimize $Z = 2x_1 + x_2$ subject to $x_1 \ge 2$ $3x_1 + 4x_2 \le 24$ $4x_1 + 3x_2 \ge 12$ |
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| | Dual S An Ex | Simj amj | plex ple. | а Ме сс | ethc ontd | od: | | | | |
|---|--|-----------------------|--------------|------------|-------------------|------------|----------------|--------|----|------|
| | Successive iterations: | | | | | | | | | |
| | Iteration | Basis | z | <i>X</i> , | <i>X</i> , | Vari x, | ables | | Xe | - b, |
| | | z | 1 | 0 | 0 | -2/3 | 0 | -1/3 | 0 | 16/3 |
| | | <i>x</i> ₁ | 0 | 1 | 0 | -1 | 0 | 0 | 0 | 2 |
| | 3 | X_4 | 0 | 0 | 0 | -7/3 | 1 | 4/3 | 0 | 38/3 |
| | | <i>x</i> ₂ | 0 | 0 | ı | 4/3 | 0 | -1/3 | 0 | 4/3 |
| | | X ₆ | 0 | 0 | 0 | 11/3 | 0 | (-2/3) | 1 | -1/3 |
| | | Ra | tios → | | | | | 0.5 | | |
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| | Dua An | al Sir Exar | npl npl | ex e | Me .co | thc ntd | od: I. | | | | |
|----|--|----------------|------------|---------|----------------|------------|-------------|-------------|-------|---------|---------------------|
| | Successive iterations: | | | | | | | | | | |
| | | Iteration | Basis | Z | X ₁ | .X.1 | Varia X1 | ables Xa | Xs | Na | <i>b</i> , |
| | | | Z | 1 | 0 | 0 | 2.5 | 0 | 0 | -0.5 | 5.5 |
| | | | x_1 | 0 | I | 0 | -1 | 0 | 0 | 0 | 2 |
| | | 4 | X_4 | 0 | 0 | 0 | 5 | I. | θ | 2 | 12 |
| | | | X_2 | 0 | 0 | I | -0.5 | 0 | 0 | -0.5 | 1.5 |
| | | | x_{5} | 0 | 0 | 0 | -5.5 | 0 | ı | -1.5 | 0.5 |
| | | | Ra | tios → | | | | | | | |
| | As all the <i>b</i> , are positive, optimum solution is reached. Thus, the optimal solution is $Z = 5.5$ with $x_1 = 2$ and $x_2 = 1.5$ | | | | | | | | | | |
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| Problems | | | | |
|---------------------------------------|---|--|--|--|
| Write the d | ual for the following | LP problems | | |
| Problem 1 Maximize $f = 5x - 2x$ | Problem 2 Minimize $f = x - 4y$ | Problem 3 | | |
| Maximizer 20 | $\frac{1}{1}$ | Maximize $f = x - 4y$ | | |
| $3x + 2y \ge 6$ $x - y \le 6$ | $\begin{array}{l} x - y \ge -4 \\ 4x + 5y \le 45 \end{array}$ | $\begin{array}{rcl} x - y \ge -4 \\ 4x + 5y \le 45 \end{array}$ | | |
| $9x + 7y \le 108$ $3x + 7y \le 70$ | $5x - 2y \le 20$ $5x + 2y \le 10$ | $5x - 2y \le 20$ $5x + 2y \ge 10$ x > 0, y is unrestricted in sign | | |
| $2x - 5y \ge -35$ $x \ge 0, y \ge 0$ | $x \ge 0, y \ge 0$ | | | |
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| | LP formulation problem | | | | | | | | |
|---|---|---|--|--|--|--|--|--|--|
| Two quar units yield units the a F, H | Two types of crops can be grown in a particular irrigation area each year. Each unit quantity of yield of crop A produced can be sold for a price P_A and requires W_A units of water, L_A units of land, F_A units of fertilizer and H_A units of labour. Similarly, yield from crop B can be sold at a unit price of P_B and requires W_B , L_B , F_B , and H_B units of water, land, fertilizer and labour respectively per unit of crop. Assume that the available quantity of water, land, fertilizer and labour respectively per unit of soft as of each of the burgers but should be produced in order to resuming total income. | | | | | | | | |
| | Decision variables: X _A and X _B - Quantity of yield from crops A and B respectively | | | | | | | | |
| | Objective Function: $P_A X_A + P_B X_B$ | | | | | | | | |
| | Subject to: | | | | | | | | |
| | Water availability constraint | $W_A X_A + W_B X_B \leq W$ | | | | | | | |
| | Land availability constraint | $L_A \hspace{0.1in} X_A \hspace{0.1in} + \hspace{0.1in} L_B \hspace{0.1in} X_B \hspace{0.1in} \leq L$ | | | | | | | |
| | $\label{eq:Fertilizer} \mbox{Fertilizer availability constraint} \qquad \mbox{F}_A \ \ X_A + \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $ | | | | | | | | |
| | Labour availability constraint | $H_A X_A + H_B X_B \leq H$ | | | | | | | |
| | Non-negativity constraints | $X_A \ge 0$ and $X_B \ge 0$ | | | | | | | |
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