


Hydrologic Variability and Uncertainty Analysis through Hydroclimatic Teleconnection



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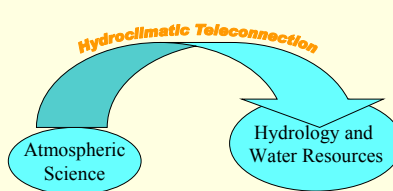
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Outline

- **Introduction**
 - El Niño-Southern Oscillation (ENSO)
 - Equatorial Indian Ocean Oscillation (EQUINOO)
- **Hydroclimatic teleconnection for Indian subcontinent**
 - Bayesian dynamic modeling of Indian summer monsoon rainfall
 - Copula: Nonparametric scale-free dependence
- **Hydroclimatic teleconnection at basin-scale**
 - Variability of basin-scale hydrologic variables
 - Forecast of monthly streamflow
- **Optimal reservoir operation with climate inputs**
- **Conclusions**

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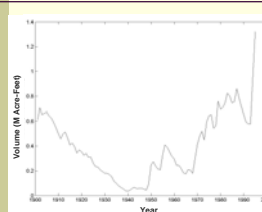
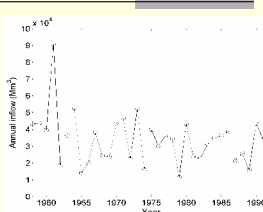
Introduction



Hydroclimatic Teleconnection: The significant association between hydrologic events and large-scale atmospheric circulation patterns, which are widely separated across the globe, is referred as 'hydroclimatic teleconnection'.

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Natural variability of hydrologic variables and hydroclimatic teleconnection

- It is recently being established that temporal structure of hydrologic time series is significantly forced by large-scale atmospheric circulation patterns through **hydroclimatic teleconnection** (Jain and Lall, 2001)

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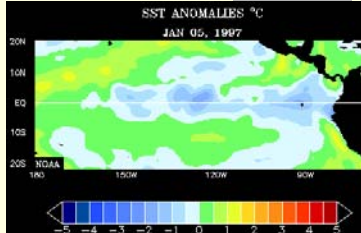
Major Issues/Challenges

- **Dynamic nature** of cause-effect relationship between hydrologic time series and large-scale circulation is to be captured.
- **Uncertainty** associated with the prediction to be addressed
- Consideration of **nonstationarity** in time series, expected under climate change scenario.
- **'Large-Scale' to 'Basin-Scale'**: It is necessary to establish the link.
- Being most essential for Hydrology and Water Resources, responses of **'basin-scale'** hydrologic variables to **'large-scale'** atmospheric circulation will be investigated
- Use of such relationship with a goal to **improve the prediction performance** of hydrologic time series.

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El Niño-Southern Oscillation (ENSO)

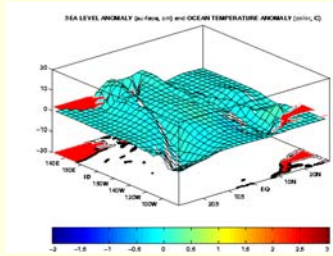
- **El Niño-Southern Oscillation (ENSO)** is the coupled Ocean-atmosphere mode of tropical Pacific Ocean (Cane, 1992)
- Attempts were made to forecast hydrologic variables, like rainfall, streamflow, etc., using ENSO information all over the world (Dracup and Kahya, 1994; Eltahir, 1996; Jain and Lall, 2001).



Source: NOAA

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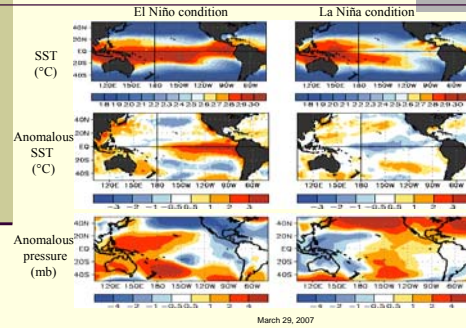
El Niño-Southern Oscillation (ENSO)



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Source: NOAA
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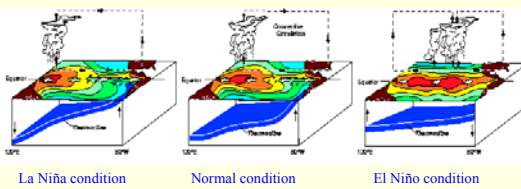
El Niño-Southern Oscillation (ENSO)



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Source: NOAA
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Change in Atmospheric Circulation



La Niña condition

Normal condition

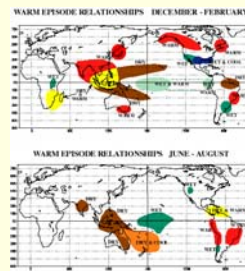
El Niño condition

Source: NOAA

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Impact of El Niño



Rainfall deficiencies

Africa, Indian Subcontinent, Northern China, Australia, Northern South America and the Caribbean

Low river discharge

Nile (Egypt), Senegal (Senegal), Orange (South Africa), Krishna (India), Murray-Darling (Australia) and Amazon (Brazil) river system

Surplus rainfall

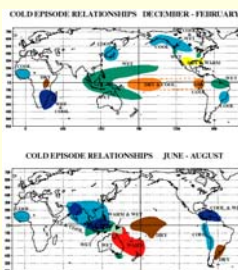
Western Europe, Eastern Africa, Western Cape of South Africa, Gulf regions of the United States and northern Mexico and central Chile.

Sources: NOAA
Allan et al., 1996

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Impact of La Niña



Increased Rainfall

Africa, Indian Subcontinent, Northern China, Australia, Northeastern South America

High River Discharge

Nile, Senegal, Orange, Krishna, Murray-Darling and Amazon

Enhanced Monsoonal/ Tropical-linked summer rainfall

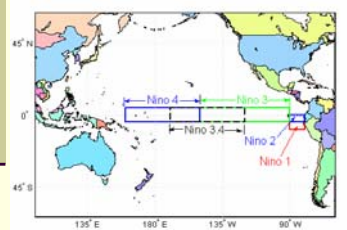
Southern Africa and India, and prominent cloud band influences lead to rainfall surplus regions over southern Australia and southern Africa

Sources: NOAA
Allan et al., 1996

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Niño Regions

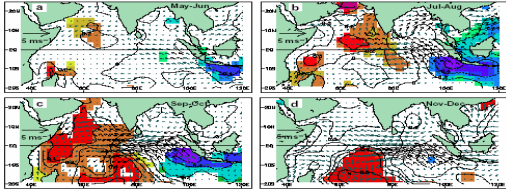


1. Niño 3.4 sea surface temperature anomaly (Niño 3.4 SSTA) is best correlated with Indian summer monsoon rainfall (ISMR)
2. Three months running mean of Niño 3.4 SSTA is known as Oceanic Niño Index (ONI)

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Indian Ocean Dipole (IOD) mode



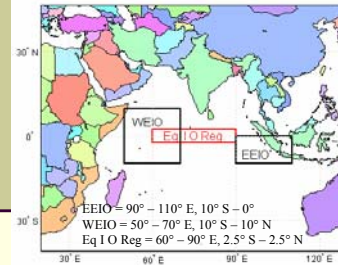
A pattern of internal variability with anomalously low sea surface temperatures near Sumatra and high sea surface temperatures in the western Indian Ocean, with accompanying wind and precipitation anomalies

Source: Saji et al., Nature, 1999

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Equatorial Indian Ocean Oscillation (EQUINOO)



Atmospheric component of Indian Ocean Dipole (IOD) Mode is known as EQUINOO.

EQUINOO is defined as the oscillation between two opposite states of convection over EEIO and WEIO.

Equatorial zonal wind index (EQWIN) is considered as a measure of this which is the negative of the anomaly of zonal wind at Eq. I O Reg.

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Impact of IOD/ EQUINOO

IOD plays an important role as a modulator of the Indian summer monsoon rainfall (ISMR) Whenever the ENSO-ISMR correlation is low (high), the IOD-ISMR correlation is high (low) (Ashok et al., 2001)

Indian summer monsoon rainfall is associated not only with ENSO, but also with EQUINOO (Gadgil et al., 2003)

Examples:	Year	ENSO	EQUINOO	ISMR
	1983, 1994	El Niño	+ve	excess
	1979, 1985	La Niña	-ve	drought
	2002	El Niño	-ve	severe drought

Composite Index between ENSO and EQUINOO has more power to predict ISMR (Gadgil et al., 2004)

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Bayesian Dynamic Linear Model (BDLM)

Important Features

- Dynamic nature of the model helps to capture the time varying relationship between climate information and hydrologic variables
- Allows incorporation of exogenous inputs
- Relaxation of stationarity assumption
- Allowance for on-line external intervention
- Probabilistic Forecast

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BDLM for monthly summer monsoon rainfall over India*

Observation Equation: $y_{i,j} = F_{i,j}^T \theta_{i,j} + v_{i,j}$ $v_{i,j} \sim N[0, V]$

where $F_{i,j} = \begin{bmatrix} 1 \\ f * EN_{i,j-k} \\ (1-f) * EQ_{i,j-k} \end{bmatrix}$ and $\theta_{i,j} = \begin{bmatrix} \bar{y}_j \\ \theta_{i,j}^m \\ \theta_{i,j}^e \end{bmatrix}$

System Equation: $\theta_{i,j} = \theta_{i,j-1} + \omega_{i,j}$ for $\forall i$ and $j = 2, \dots, 12$
 $\theta_{i,j} = \theta_{i-1,12} + \omega_{i,j}$ for $\forall i$ and $j = 1$

where $\omega_{i,j} \sim T_n[0, W_{i,j}]$ and $n = (i-1)*12 + j - 1$

Initial Information $(\theta_{i,0} / D_{i,0}) \sim T_n[m_{i,0}, C_{i,0}]$ and $(\phi / D_{i,0}) \sim G[m_{i,0} / 2, d_{i,0} / 2]$

where $\phi = V^{-1}$

* Journal of Geophysical Research – Atmospheres, AGU, 2006

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BDLM for summer monsoon rainfall over India...contd.

At Time step $(i, j-1)$ $(\theta_{i,j-1} / D_{i,j-1}) \sim T_n[m_{i,j-1}, C_{i,j-1}]$ and $(\phi / D_{i,j-1}) \sim G[m_{i,j-1} / 2, d_{i,j-1} / 2]$

Prior distribution for $\theta_{i,j}$ $(\theta_{i,j} / D_{i,j-1}) \sim T_n[m_{i,j-1}, R_{i,j}]$ where $R_{i,j} = C_{i,j-1} + W_{i,j}$

$W_{i,j}$ is the system evolution variance. It is practically difficult to assign the sequence of evolution variance $\{W_{i,j}\}$ without relating it to some previous known variance.

$$R_{i,j} = C_{i,j-1} / \delta \quad (0 < \delta \leq 1)$$

$$\text{Thus } W_{i,j} = C_{i,j-1} (\delta^{-1} - 1)$$

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BDLM for summer monsoon rainfall over India...contd.

One-step ahead forecast distribution $(Y_{i,j} / D_{i,j-1}) \sim T_n[F_{i,j}, Q_{i,j}]$

where $F_{i,j} = \bar{Y}_j + EN_{i,j-k} * f * m_{i,j-1}^{eq} + EQ_{i,j-2} * (1-f) * m_{i,j-1}^{eq}$

$Q_{i,j} = (EN_{i,j-k} * f)^2 * R_{i,j}^{eq} + (EQ_{i,j-2} * (1-f))^2 * R_{i,j}^{eq} + S_{i,j-1}$

$S_{i,j-1} = \frac{d_{i,j-1}}{n_{i,j-1}}$

Posterior distribution for $\theta_{i,j}$ $(\theta_{i,j} / D_{i,j}) \sim T_n[m_{i,j}, C_{i,j}]$

where $m_{i,j} = m_{i,j-1} + A_{i,j} e_{i,j}$ $C_{i,j} = R_{i,j} S_{i,j} / Q_{i,j}$ $S_{i,j} = d_{i,j} / n_{i,j}$

$e_{i,j} = Y_{i,j} - f_{i,j}$ $A_{i,j}^{eq} = EN_{i,j-k} * f * R_{i,j} / Q_{i,j}$ $A_{i,j}^{eq} = EQ_{i,j-2} * (1-f) * R_{i,j} / Q_{i,j}$

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BDLM for summer monsoon rainfall over India...contd.

Distributional form of scale parameter ϕ at time step (i, j)

$(\phi / D_{i,j}) \sim G[n_{i,j} / 2, d_{i,j} / 2]$

where $n_{i,j} = n_{i,j-1} + 1$ $d_{i,j} = d_{i,j-1} + S_{i,j-1} e_{i,j}^2 / Q_{i,j}$

Data

Large Scale circulation Information: ENSO index and EQUINOO index

Target Variable: Monthly rainfall over India

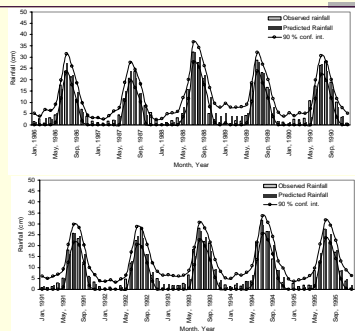
Model Calibration Period : 1958 – 1985

Model Testing Period : 1986 – 2003

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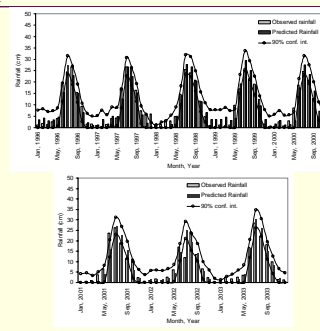
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Model Performance during testing period 1986 – 2003



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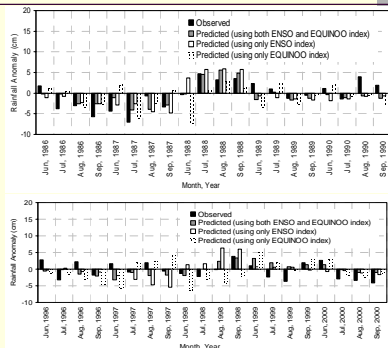
Model Performance during testing period 1986 – 2003



Correlation coefficient between observed and predicted rainfall during monsoon months = 0.82

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Model Performance during testing period 1986 – 2003



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Summary

- Efficacy of the BDLM to capture the dynamic relationship between monthly rainfall anomaly and circulation indices is established.
- Predictions of uncertain future values are available in a distributional form.
- Concurrent influence of ENSO and EQUINOO index on monthly rainfall variation is established.
- Unusual recent experiences are satisfactorily explained by this approach, for instance, 1997, 2002 etc.
- Both ENSO and EQUINOO have significant influence on monthly Indian summer monsoon rainfall.

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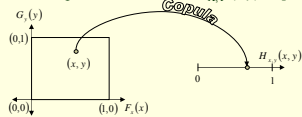
Scale-free dependence between hydroclimatic variables using Copula

Copula

A copula is a function that joins or couples multiple distribution functions to their one-dimensional marginal distribution functions.

Let X and Y be a pair of 'Random Variables' with cdf as $F_X(x)$ and $G_Y(y)$. Also let their joint cdf as $H_{X,Y}(x,y)$.

Each pair (x,y) leads to a point in the unit square $[0,1] \times [0,1]$. And this ordered pair in turn corresponds to a number $H_{X,Y}(x,y)$ in $[0,1]$.



This correspondence is indeed a function. This function is known as Copula

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Introduction to Copula

Sklar's Theorem

Let, $H_{X,Y}(x,y)$ is a Joint distribution function with margins $F_X(x)$ and $G_Y(y)$. Then there exists a copula C such that for all x, y in \bar{R} ,

$$H_{X,Y}(x,y) = C(F_X(x), G_Y(y))$$

If F and G are continuous, then C is unique; otherwise, C is uniquely determined on $\text{Ran}F \times \text{Ran}G$.

Conversely, if C is a copula and $F_X(x)$ and $G_Y(y)$ are CDFs, then

$$H_{X,Y}(x,y) = C(F_X(x), G_Y(y))$$

is the joint CDF with margins $F_X(x)$ and $G_Y(y)$

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Archimedean Copula

A copula that can be expressed in terms of

$$C(u,v) = \varphi^{-1}(\varphi(u) + \varphi(v))$$

known as 'Archimedean copula', where φ is a strictly decreasing, continuous function and φ is known as generator of Copula

φ^{-1} is known as 'pseudo inverse' and defined as

$$\varphi^{-1}(t) = \begin{cases} \varphi^{-1}(t), & 0 \leq t \leq \varphi(0) \\ 0, & \varphi(0) \leq t \leq \infty \end{cases}$$

Expression for Kendall's τ reduced to $\tau = 1 + 4 \int_0^1 \frac{\varphi(u)}{\varphi'(u)} du$

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Archimedean Copula

	$C_\theta(u,v)$	$\varphi_\theta(t)$	$\theta \in$
Clayton	$[\max(u^{-\theta} + v^{-\theta} - 1, 0)]^{-1/\theta}$	$\frac{1}{\theta}(t^{-\theta} - 1)$	$[1, \infty) \setminus \{0\}$
Frank	$-\frac{1}{\theta} \ln \left(1 + \frac{(e^{-\theta u} - 1)(e^{-\theta v} - 1)}{e^{-\theta} - 1} \right)$	$-\ln \left(\frac{e^{-\theta t} - 1}{e^{-\theta} - 1} \right)$	$(-\infty, \infty) \setminus \{0\}$
Ali-Mikhail-Haq	$\frac{uv}{1 - \theta(1-u)(1-v)}$	$\ln \frac{1 - \theta(1-t)}{t}$	$[-1, 1)$
Gumbel-Hougaard	$\exp \left\{ - \left[(-\ln u)^\theta + (-\ln v)^\theta \right]^{1/\theta} \right\}$	$(-\ln t)^\theta$	$[-1, \infty)$

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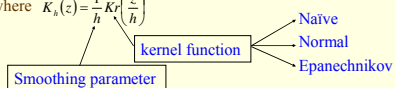
Copula-based method to capture scale-free dependence pattern

Nonparametric estimate of probability density

Kernel density estimator is most popular for estimation of nonparametric density

$$\hat{f}(x) = \frac{1}{n} \sum_{i=1}^n K_h(x - X_i)$$

where $K_h(z) = \frac{1}{h} K\left(\frac{z}{h}\right)$



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Copula-based method to capture scale-free dependence pattern

Step 1

Sample estimate of Kendall's Tau

$$\hat{\tau} = P[(x_i - x_j)(y_i - y_j) > 0] - P[(x_i - x_j)(y_i - y_j) < 0] = \frac{c}{n C_2} - \frac{d}{n C_2} = \frac{c-d}{n C_2}$$

Step 2

Sample estimate of Kendall's Tau is plugged in the following equation

$$\tau = 1 + 4 \int_0^1 \frac{\varphi_\theta(u)}{\varphi'_\theta(u)} du$$

Estimate of θ is available for a particular Copula

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Copula-based method to capture scale-free dependence pattern

Step 2 ..contd

Simulation with a particular Copula (Genest and MacKay, 1986b)

- $\varphi^{[-1]}(\bullet)$, $\varphi'(\bullet)$ and $\varphi^{(-1)}(\bullet)$ are obtained
- $U = [\sim Un(0,1)]$; $T = [\sim Un(0,1)]$
- $S = \varphi(U)/T$; $W = \varphi^{(-1)}(S)$
- $V = \varphi^{[-1]}(\varphi(W) - \varphi(U))$
- The pair U and V are the simulated pair, preserving the dependence structure
- U and V are then transformed by inverse cumulative distribution function

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Copula-based method to capture scale-free dependence pattern

Step 3

Selection of the most appropriate copula (Genest and Rivest, 1993; Zhang and Singh, 2006)

$$\text{Parametric } K(z) = z - \frac{\varphi(z)}{\varphi'(z^*)}$$

Nonparametric $K_n(z)$ = the fraction of $z_i \leq z$

$$\text{where } z_i = \frac{\text{Number of } (x_j, y_j) \text{ such that } x_j < x_i \text{ and } y_j < y_i}{(N-1)} \quad \begin{matrix} i = 1, \dots, N \\ j = 1, \dots, N \\ j \neq i \end{matrix}$$

A scatter plot between $K(z)$ and $K_n(z)$ is prepared

The better the fit, the closer the corresponding scatter to a 45° line through origin
Lowest value of sum of square errors (SSE) from the 45° line through origin

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Copula-based method to capture scale-free dependence pattern

Step 4

After selecting the best copula, a large number ($\sim 10^4$) of jointly distributed values are numerically simulated. These values are back transformed by using the corresponding non-parametrically estimated cumulative probability density.

Step 5

Keeping any observed value of climate precursors at the centre, a sufficiently 'small' window around it, is selected. Statistical properties of the simulated values of the response variable, lying within this window, are investigated through box plot. The median of these values is used as a prediction, corresponding to the observed value of the climate precursor. The interquartile range (75th percentile – 25th percentile) of these values indicates the associated uncertainty

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Dependence of ISMR on ENSO and EQUINO

➤ Target Time series → Monthly all India rainfall

➤ Exogenous Input → Combined index of ENSO and EQUINO

$$\text{Combined index } CI_{i,j} = c_1 EN_{i,j-\kappa} + c_2 EQ_{i,j-\lambda}$$

where $c_1 = 0.61$

$c_2 = 0.29$

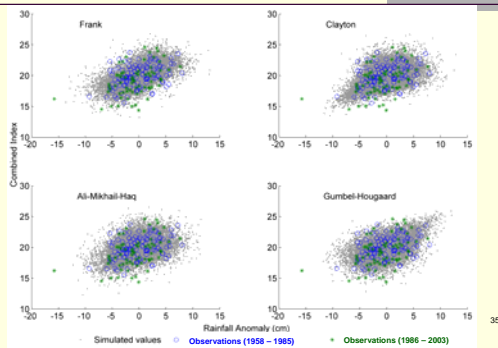
$\kappa = 2$

$\lambda = 1$

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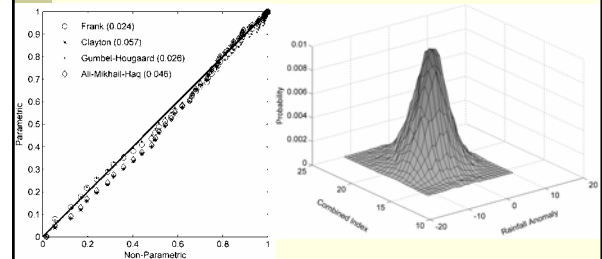
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Simulation with different copulas



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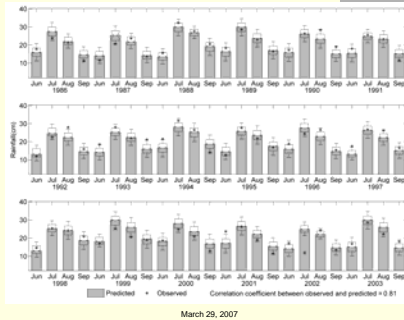
Selection of an appropriate Copula and corresponding joint density



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Comparison between observed and predicted rainfall



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Summary

- A new method is proposed to capture the dependence between the teleconnected hydroclimatic variables for successful prediction of the response variable
- While capturing the relationship, uncertainty associated with the relationship is also provided
- Nonparametric estimates of probability density of the data sets are used in the proposed method
- The proposed method is general in many aspects and can therefore be applied to similar studies irrespective of distributional form, associated uncertainty and nature of dependence.

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Monthly Composite Index (MCI) of ENSO and EQUINOX over homogeneous monsoon regions of India

Association of MCI with monthly variation of ISMR considering lagged relationship

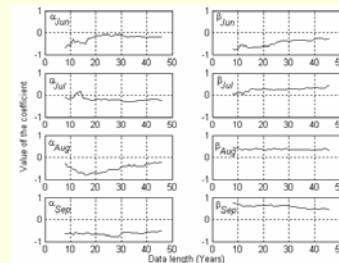
Rainfall anomaly	Month of		Equation for MCI	Correlation coefficient [#]
	ENSO	EQUINOX		
Jun	Mar	Mar	$MCI = -0.18 * NINO_{Mar} - 0.29 * EQWIN_{Mar}$	0.38
Jul	Jun	Jun	$MCI = -0.24 * NINO_{Jun} + 0.43 * EQWIN_{Jun}$	0.54
Aug	Jul	Jul	$MCI = -0.24 * NINO_{Jul} + 0.28 * EQWIN_{Jul}$	0.35
Sep	Aug	Jul	$MCI = -0.53 * NINO_{Aug} + 0.44 * EQWIN_{Jul}$	0.65

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Coefficients of MCI equations for varied length of data period

$$MCI = \alpha \cdot EN + \beta \cdot EQ$$

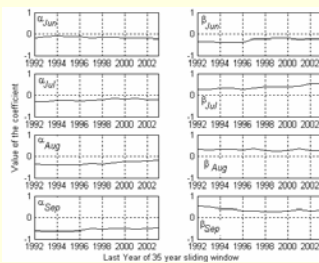


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Coefficients of MCI equation for 35 years sliding window

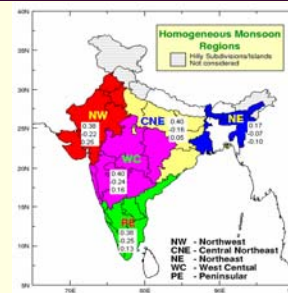
$$MCI = \alpha \cdot EN + \beta \cdot EQ$$



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Spatial Variation of Monthly Composite Index and Rainfall*



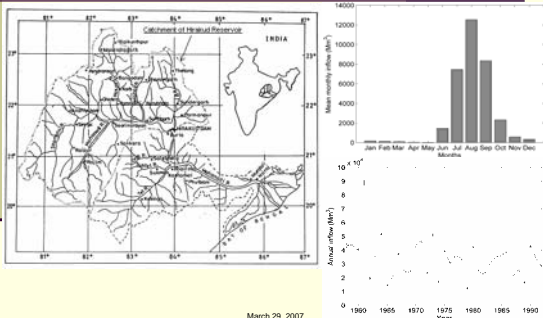
Three different correlation coefficients are shown for each region in a vertical sequence. These are between the monthly rainfall anomaly during monsoon months and (1) the MCI, (2) the ENSO index and (3) the EQUINOX index, respectively

* Atmospheric Science Letters, Royal Meteorological Society (RMets), UK, 2006

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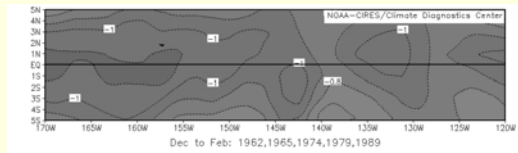
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Large-scale circulation phenomena and basin-scale hydrologic variables



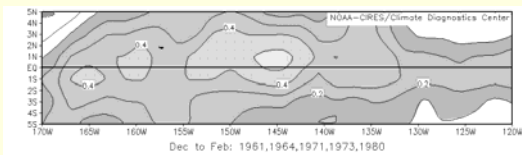
ENSO and Hirakud Inflow

- Composite picture of SST anomalies (°C) from Niño 3.4 region for five lowest flow years



ENSO and Hirakud Inflow

- Composite picture of SST anomalies (°C) from Niño 3.4 region for five highest flow years



Correlation coefficients

- Correlation coefficients of monsoonal inflow into Hirakud reservoir with i) ONI and ii) EQWIN for different premonsoon periods

Period	Correlation Coefficient with ONI	Correlation Coefficient with EQWIN
Dec, Jan, Feb	0.207	-0.194
Jan, Feb, Mar	0.153	-0.245
Feb, Mar, Apr	0.053	-0.239
Mar, Apr, May	-0.040	-0.077

* Month of previous year

Combined Association

$$\text{Composite Index } CI = \alpha \cdot EN + \beta \cdot EQ$$

By least square technique

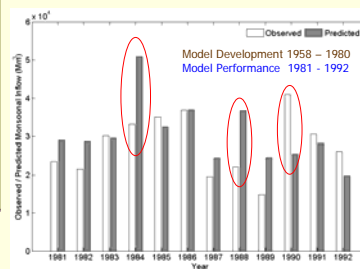
$$CI = 0.366 EN - 0.577 EQ$$

CI range	NL (CP)	NM (CP)	NH (CP)
< -0.3 (Lower 1/3 rd)	5 (0.71)	2 (0.29)	0 (0.0)
-0.3 to 0.3 (Middle 1/3 rd)	5 (0.30)	5 (0.30)	7 (0.40)
> 0.3 (Upper 1/3 rd)	3 (0.27)	2 (0.18)	6 (0.55)

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Prediction of inflow into Hirakud reservoir*



- Monsoonal inflow is under-predicted for the year 1990 and over-predicted for the years 1984 and 1988

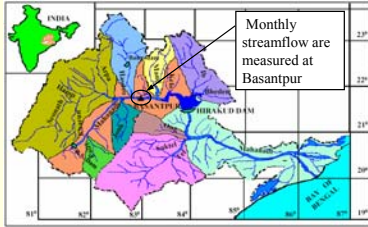
For the rest of the years, the prediction performance is quite good

* Journal of Hydrologic Engineering, ASCE, in review

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Sub-basin Map of Mahanadi River



At monthly time-scale, the hydroclimatic teleconnection between basin-scale streamflow and large-scale atmospheric circulation pattern is more complex.

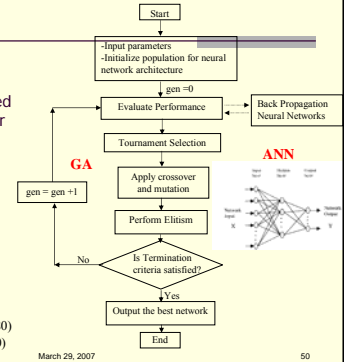
Genetic Algorithm based Evolutionary Optimizer is adopted to obtain optimal Artificial Neural Network (ANN) architecture, which is used to capture the complex relationship

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GA – ANN Approach

Genetic Algorithm Optimized Artificial Neural Network for Streamflow Prediction with Climate Inputs



Training Data: 23 years (1958 – 1980)
Testing Data: 10 years (1981 – 1990)

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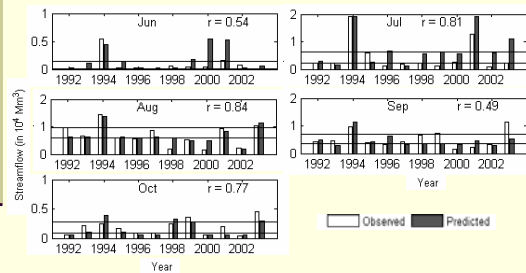
Performance for three different cases@

Month	Considering only streamflow information of previous month(s)			Considering only large-scale atmospheric circulation information			Considering both streamflow (if necessary) and large-scale atmospheric circulation information		
	Inputs*	Best Network	Model Performance ^c	Inputs*	Best Network	Model Performance ^c	Inputs*	Best Network	Model Performance ^c
Jun →	May SF	1-2-2-1	-0.030 833.0 1500.3	Mar EN Mar EQ	2-4-5-3-1	0.542 1209.4 1926.4	Mar EN Mar EQ	2-4-5-3-1	0.542 1209.4 1926.4
Jul →	Jun SF	1-2-2-2	0.731 4312.8 5025.6	Jun EN Jun EQ	2-3-2-1	0.298 5643.6 6059.4	Jun SF Jun EN Jun EQ	3-3-5-1	0.813 3570.9 4425.2
Aug →	Jul SF	1-2-3-1-1	0.412 2929.2 3575.7	Jul EN Jul EQ	2-2-1	0.511 2721.5 3225.6	Jul SF Jul EN Jul EQ	3-6-5-1	0.836 1486.0 2008.5
Sep →	Jul SF Aug SF	2-2-3-1-1	0.321 2331.9 3260.2	Aug EN Aug EQ	2-3-1-2-1	0.402 1877.1 2719.7	Jul SF Aug SF Aug EN Aug EQ	4-3-2-1	0.493 2101.0 2635.6
Oct →	Sep SF	1-2-1	0.838 611.6 761.4	Sep EN Sep EQ	2-4-3-1	0.372 898.8 1228.1	Sep SF Sep EN Sep EQ	3-5-1	0.765 742.2 926.5

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Network Performance for Testing Period (1992 – 2003)



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Network Performance for Testing Period (1992 – 2003)

Observed Category of Streamflow	Predicted Category of Streamflow		
	Low	Normal	High
Low	12	6	3
Normal	3	20	4
High	0	3	9

Heidke skill score, $HSS = (CF - CF_{rand}) / (N - CF_{rand}) = 0.525$ (Wilks, 2006)

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Malaprabha Inflow Forecast Models

Annual Inflow Forecast

$$Q_t = f(Nino_{feb}, Nino_{mar}, Q_{t-2}, Q_{t-1})$$

Monthly Inflow Forecast

$$Q_t = f(Nino_{t-2}, Nino_{t-1}, Q_{t-2}, Q_{t-1})$$

Ten-daily inflow Forecast Model

$$Q_t = f(Rain_{t-1}, Q_{t-2}, Q_{t-1})$$



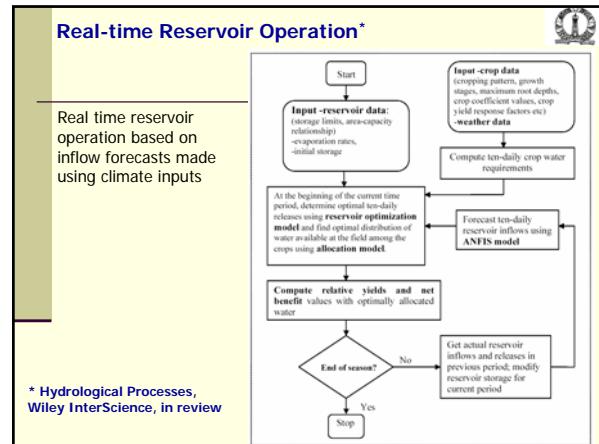
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Malaprabha Inflow Forecast Models

Model	Performance measure	PSOENN			BPNN			ANFIS		
		Training	Validation	Testing	Training	Validation	Testing	Training	Validation	Testing
Annual	RMSE	219.6361	309.127	213.7561	234.384	348.4827	292.4613	181.3062	285.7193	271.6191
	MAE	149.8344	208.4584	161.9773	152.4845	306.4618	266.8942	109.9852	232.5193	237.6673
	r	0.8227	0.7575	0.6327	0.9185	0.6583	0.5935	0.9516	0.7922	0.6682
	CE	0.8803	0.2165	0.3171	0.8720	0.3256	0.2183	0.9023	0.4325	0.2467
Monthly	RMSE	124.2218	88.2118	169.6542	89.5654	98.1284	201.8452	79.0521	74.3287	127.7455
	MAE	72.9947	62.2102	108.9456	64.5592	76.5942	129.9456	45.0099	48.407	90.3816
	r	0.8952	0.8582	0.6632	0.9128	0.65981	0.5962	0.9484	0.9023	0.6942
	CE	0.6924	0.7118	0.2313	0.6984	0.5784	0.3384	0.8754	0.8096	0.1834
Monsoon season	RMSE	7.5010	6.6121	5.0251	6.8010	7.2121	7.864	4.8216	5.5417	6.9679
	MAE	4.5204	4.7637	3.5612	4.446	5.932	4.9318	3.0864	4.0361	4.1862
	r	0.8814	0.7419	0.6467	0.8923	0.5897	0.5863	0.9256	0.8278	0.6213
	CE	0.6299	0.5464	0.4221	0.7639	0.6954	0.32949	0.8471	0.6814	0.469
Non-monsoon season	RMSE	48.1687	55.6173	42.7136	56.5813	62.6837	47.5464	41.1265	53.0554	50.6064
	MAE	27.7492	28.154	24.7922	31.8873	29.856	26.8829	23.2053	25.0324	28.3243
	r	0.9106	0.7634	0.6315	0.8964	0.751	0.6648	0.9296	0.7781	0.5981
	CE	0.692	0.5579	0.3391	0.6234	0.5892	0.3251	0.6494	0.5977	0.3158
Ten daily	RMSE	2.4704	2.5779	2.0603	3.0782	3.8574	2.8569	2.1115	2.158	1.7649
	MAE	1.7180	1.6349	1.5807	2.3351	2.5694	1.6963	1.3777	1.4912	1.4354
	r	0.8915	0.7563	0.6152	0.8625	0.6945	0.5962	0.9126	0.7955	0.6226
	CE	0.5328	0.4455	0.2333	0.6482	0.6195	0.2259	0.6587	0.6114	0.4319

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Conclusions

- ❑ Bayesian dynamic linear model (BDLM) is newly introduced to the field of hydroclimatology, which is able to capture the time varying dynamic relationship and quantify the uncertainty associated with the predicted values.
- ❑ A Copula-based method is able to capture the scale-free dependence pattern and provides a nonparametric way to predict the response variable using the information from causal force.
- ❑ Mahanadi River basin is investigated for the basin-scale hydroclimatic teleconnection. Hydroclimatic association at seasonal scale between monsoonal inflow into Hirakud reservoir on Mahanadi River and large-scale circulation phenomena is established.
- ❑ At monthly scale, streamflow at Basantpur site in Mahanadi River basin is predicted using GA-ANN approach.
- ❑ Inflow forecasts thus obtained are useful for better water resources management.

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